

# 2.2 Equivalence of fractions and decimals

Fract	tions					
nust hav	ve the san	ne denom	inator			
5	7	2	3			
6	$\overline{12}$	3	4			
T	T	T	Ļ			
10	▼ 7	v Q	8			
$\frac{10}{12}$	$\frac{7}{12}$	$\frac{1}{12}$	$\frac{0}{12}$			
12	12	12	12			
the fra	ctions ca	n be ord	ered			
Decir	nals					
hem all ·	the same	number o	f diaits			
0.3	0.304	0.32	0.33			
⊥ ⊥	⊥		, e.e.e ⊥			
₹ 300	0 304	0 320	0 3 3 0			
0.300 $0.304$ $0.320$ $0.330$						
Now the decimals can be ordered						
Course to be transferred to a strength						
dooin		veen m	actions a			
Decimals to tractions						
2 4 7 5						
<b>▼</b>						
$\frac{4}{10}$						
$10 \checkmark$						
	· / I					
	Fract nust hav $\frac{5}{6}$ $\frac{10}{12}$ the fract Decir hem all 0.3, $\frac{10}{12}$ the decir convert decin nals to 2.2	Fractions nust have the sam $\frac{5}{6} \qquad \frac{7}{12}$ $\downarrow \qquad \downarrow$ $\frac{10}{12} \qquad \frac{7}{12}$ The fractions can be fractions can Decimals hem all the same for the same fo	Fractions nust have the same denom $\frac{5}{6} \qquad \frac{7}{12} \qquad \frac{2}{3}$ $\downarrow \qquad \downarrow \qquad \downarrow$ $\frac{10}{12} \qquad \frac{7}{12} \qquad \frac{9}{12}$ The fractions can be ord Decimals hem all the same number of 0.3, 0.304, 0.32 $\downarrow \qquad \downarrow \qquad \downarrow$ $300 \qquad 0.304 \qquad 0.320$ The decimals can be ordet Convert between from decimals nals to fractions 2.475 $\downarrow \qquad \downarrow \qquad \downarrow$			

1000 <u>Fractions to decimals</u> - by changing

5

e.g. 
$$\frac{4}{5} = \frac{8}{10} = 0.8$$
  
e.g.  $\frac{9}{12} = \frac{3}{4} = 0.75$   
Fractions to decimals - by dividing  
e.g.  $\frac{3}{8} = 3 \div 8 = 0.375$ 

## 2.3 Order of operations



## 2.4 Powers and roots

$$4^2$$
 - we say 4 squared or the square of 4  
- It means  $4x4 = 16$   
 $2^3$  - we say 3 cubed or the cube of 3  
- It means  $2x2x2 = 8$   
 $3^4$  - we say 3 to the power of 4  
- It means  $3x3x3x3 = 81$   
The inverse operation for 'power' is 'root'  
 $\sqrt{16} = 4$   
 $\sqrt[3]{8} = 2$   
 $\sqrt[4]{81} = 3$   
There are keys on the calculator to all of these

# 2.5 Simplify fraction

See what number divides exactly into both the numerator and denominator

e.g. 
$$\frac{\frac{8}{12}}{\frac{12}{4}} \rightarrow \frac{2}{3}$$
  
 $\frac{2}{3}$   
 $\frac{5}{40} \rightarrow \frac{3}{8}$   
 $\frac{15}{5} \rightarrow \frac{3}{8}$ 

2.5 Simplify <u>Ratio</u>How it is written



Yellow : Red = 2 : 6

• How it can be simplified

 $\triangle \bigstar \bigstar \bigstar \bigstar \bigstar \bigstar \bigstar \bigstar \bigstar$ 

Yellow : Red = 1 : 3

• Simplify by cancelling

Examples

 $2^{+2}$ :  $6^{+2} = 1 : 3$  $10^{+5} : 15^{+5} = 2 : 3$ 

## 2.6 Fractions

Add & subtract with same denominator e.g.  $\frac{2}{3} + \frac{2}{3} = \frac{4}{3} = 1\frac{1}{3}$ Multiply is just repeated addition e.g.

**2**  $\times \frac{2}{3} = \frac{2}{3} + \frac{2}{3} = \frac{4}{3} = \mathbf{1}\frac{1}{3}$ 

2.7 Fraction of quantity with calculator					
• <u>4</u> means ÷ 5 × 4					
	5				
e.g. To find <u>4</u> of £40					
5					
$\pounds 40 \div 5 \times 4 = \pounds 40$					
E7 Percentage of guantity - NO calculator					
		-	•		
Use	50%	10%	1%		
	<b>↓</b>	Ļ	Ļ		
	÷2	÷10	÷100		

2.7 <u>Percentage of quantity-with calculator</u>	<u>:</u>   2	
• Change the percentage to a decimal $e = 8\%$ of $f = 240$ $12 \stackrel{1}{=} \%$ of $80kc$	ו	
$-0.08 \times 240$ $-0.125 \times 80$		
$-6.00 \times 240 -0.123 \times 00$	'	
- <u>10kg</u>		
80% of 52 litres	'	
= 0.8 × 52		
= 41.6 litres		
2.8 Decimals		
Add & subtract- Line up the decimal points		
Multiply - take out decimal point		
Multiply		
Put decimal point back in		
e.g. 3.2 × 0.4		
32 × 4 (remove decimal points)		
> 128 (multiply)		
> 1.28 (put decimal point back in-2 decimal places)	6	
Divide - make divisor into a whole number		
Multiply both numbers		
e.g. $2.84 \div 0.2$ (multiply both numbers by 10)		
> 28.4 ÷ 2		
> 14.1		

2.9 Order negative numbers

 $-3 \quad -2 \quad -1 \quad 0 \quad 1 \quad 2 \quad 3$   $2 \rightarrow -2 \longrightarrow We \text{ say 2 is bigger than -2}$   $-1 < 3 \longrightarrow We \text{ say -1 is less than 3}$ 

## E9 Add & Subtract Negative numbers

Remember the rules:

- When subtracting go down the number line
- When adding go up the number line
- 8 + 2 is the same as 8 2 = 6
- 8 + 2 is the same as 8 2 = 6
- 8 - 2 is the same as 8 + 2 = 10

# 2.10 <u>Number patterns</u>

Look to see how numbers are connected • Multiples Multiples of 6 are: 6, 12, 18, 24, 30... • Factors Factors of 6 are: 1, 6, 3, 2 • Prime numbers Prime numbers have only TWO factors 2, 3, 5, 7, 11, 13, 17, 29, 31, 37 ..... • Sequences 1, 4, 9, 16, 25, 36 ... are all square numbers 1, 8, 27, 64, 125 ... are all cube numbers 1, 4, 7, 10, 13, 16 ... increase b 3 each time

## 2.11 Manipulate expressions

Only like terms can be added & subtracted e.g. a + 2b cannot be added  $a^2 - 2a$  cannot be subtracted a + 2a = 3a $5a^2 - 2a^2 = 3a^2$ Terms can be simplified when multiplying e.g.  $a \times b = ab$  $2a \times 3a = 6a^2$ 

## E2.12 <u>Solve equations – by balancing</u>

- e.g. 2x 3 = 7 (add 3 to each side) 2x = 10 (divide both sides by 2) x = 5
- e.g.  $\underline{x}$  +1 = 5 (subtract 1 from each side)

 $\underline{x}$  = 4 (multiply both sides by 2)

 $\frac{x}{2}$  - - (multiply both sides by 2)

x = 8

# 2. 13 Symmetries





### Draw lines on to take readings

#### • Read the scale carefully

#### e.g. Read & interpret timetables

Station	Time of leaving			
Peterborough	<mark>08 44</mark>			
Huntingdon	09 01			
St Neots	09 08			
Sandy	<mark>09 15</mark>			
Biggleswade	09 19			
Arlesey	09 24			
e.g. Time taken to travel from Peterbrough to Sandy				
0844 0900	0915			
16min +	15min = 31min			

2.18 Units of measure					
• Metric units					
Length	Weight	Capacity			
10mm =1cm	1000g=1kg	1000ml=1 litre			
100cm =1m		10ml=1centilitre			
1000m=1km					
• Imperial units					
Length	Weight	Capacity			
1 inch=2.5cm	2.2 pounds≈1kg	1gallon≈4.5litres			
1 foot=30cm					
1 mile≈1 6km					

# 2.19 Area and perimeter of rectangle

 $\underline{Area}$  is the amount of space inside the outline of a shape

<u>Perimeter</u> is the length of the outline of a shape

# • Area of rectangle = length x width



Area of rectangle = 1 x w

= 8 × 3 = **24cm**<sup>2</sup>

# • Perimeter of the rectangle

Perimeter = 3 + 8 + 3 + 8 OR 2x3 + 2x8 <u>22cm</u>

2.20 <u>Probability</u>
Calculate probability
P(event) = No. of outcomes which give the event
Total number of outcomes
<ul> <li>Probability of an event NOT</li> </ul>
happening
If p(event) = p
P(event NOT happening) = 1 - p
e.g. If p(rain ) = 0.3
p(no rain = 1 - 0.3 = 0.7

## 2.21 Averages and Range

Mode – most frequent measure Median – middle measure (put them in order) Mean – total of measures ÷ no. of measures Range – Highest minus lowest measure

- Range measures how spread out the measures are
- Mode, median & mean gives an average
- The range and one of the averages is used to compare distributions

## 2.22 Find all possible outcomes

#### Outcomes can be presented:

- In a list
- In a table or sample space

#### Example of a sample space

To show all possible outcomes from spinning a spinner and rolling a dice



		Dice					
	+	1	2	3	4	5	6
ner	1	2	3	4	5	6	7
	2	3					
Spir	3	4					
	4	5					



• Here we are not told how many people are in the survey

• We can therefore only comment on proportion by comparing the sizes of sectors in each pie chart

e.g. there is a larger proportion of the population under 15 in Ireland than Greece

## It does not mean there are more people

#### 2.23 Construct a pie chart

Transport	Frequency	Angle
Car	13 × 9	117 <sup>0</sup>
Bus	4 × 9	36 <sup>0</sup>
Walk	15 x 9	135
Cycle	8 x 9	72

# Total frequency = 40 $360^{\circ} \div 40 = 9^{\circ}$ per person